

## Sintering and grain growth of rare-earth-doped ceria particles

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Rare-earth-doped ceria powders with a composition of  $\text{Ce}_{0.8}\text{R}_{0.2}\text{O}_{1.9}$  ( $\text{R}=\text{Yb}, \text{Y}, \text{Gd}, \text{Sm}, \text{Nd}$  and  $\text{La}$ ) were prepared by heating the oxalate coprecipitate. The green compacts began to shrink at  $600^{\circ}\text{C}$ – $700^{\circ}\text{C}$ . The relative density after the sintering at  $1200^{\circ}$  and  $1400^{\circ}\text{C}$  became higher for the higher green density. The samples were densified above 98% relative density by the sintering at  $1600^{\circ}\text{C}$  for 4 h and the grain sizes ( $4.7$ – $7.6\ \mu\text{m}$ ) showed a tendency to become larger with increasing ionic radius of doped rare-earth element. In the initial stage of sintering at  $700^{\circ}$ – $800^{\circ}\text{C}$ , the dominant mass transport process changed from lattice diffusion to grain boundary diffusion with heating time. The porosity during the intermediate and final stage of the sintering at  $1200^{\circ}$  and  $1400^{\circ}\text{C}$  decreased by the mass transport through lattice diffusion with grain growth.

**Key words:** Ceria, Rare-earth-doped, Sintering, Densification, Microstructure, Grain growth, Lattice diffusion, Grain boundary diffusion.

### Introduction

Solid oxide fuel cell (SOFC) has been expected as a high efficient and clean electric generator. The SOFC with  $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  as solid electrolyte is operated at  $1000^{\circ}\text{C}$ . Rare-earth-doped ceria has a higher oxygen ion conductivity than  $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  and is a candidate electrolyte for the low temperature operation [1–4]. Reducing the operation temperature is effective to increase the life time and to expand the choice of the constituent materials (electrodes or metal gas separator) of SOFC. The solid electrolyte should be dense to separate fuel gas and air. The microstructure of electrolyte affects its oxygen ion conductivity [4]. Therefore sintering and grain growth of the solid electrolyte are strictly controlled for the elevation of quality of SOFC. Inaba *et al.* reported the sintering behavior of undoped and Gd-doped ceria [5]. Chen *et al.* studied the grain growth of  $\text{CeO}_2$  [6] and the diffusibility of doped cation in  $\text{CeO}_2$  [7]. In this paper, the densification behavior and the sintering mechanisms of rare-earth-doped ceria were studied.

### Experimental Procedure

Rare-earth-doped ceria powders with a composition of  $\text{Ce}_{0.8}\text{R}_{0.2}\text{O}_{1.9}$  ( $\text{R}=\text{Yb}, \text{Y}, \text{Gd}, \text{Sm}, \text{Nd}$  and  $\text{La}$ ) were prepared by heating the oxalate coprecipitate at  $600^{\circ}\text{C}$  in air. The detailed powder preparation is described in our previous paper [8]. The size and specific surface

area of produced powder were measured by a particle size distribution analyzer with laser diffraction (Hoes & Rodes, Jeol Co., Japan) and BET surface area analyzer (Flowsorb II 2300, Simadzu Co., Japan), respectively. These powders were compacted isostatically to rectangular specimen (5 mm width, 5 mm thickness and 14 mm length) or disk (10 mm diameter and 2 mm thickness) under a pressure of 294 MPa after uniaxial dry pressing of 49 MPa. The linear shrinkage of the length of rectangular green body was monitored by thermal mechanical analyzer (TMA 8310, Rigaku Co., Japan) in air at a heating rate  $5^{\circ}\text{C}/\text{min}$ . These shrinkage data were calibrated by blank test and the reference data of  $\alpha\text{-Al}_2\text{O}_3$ . The bulk density of sintered sample was measured by the Archimedes method using distilled water. The theoretical density was calculated from the lattice parameter measured by X-ray diffraction using NaCl as a standard substance [8]. The microstructure of sintered sample was observed by a scanning electron microscope (SEM, SM-300, Topcon Co. Ltd., Japan). The average grain size of sintered body was measured over 200 grains by the linear intercept method and multiplied by 1.56 to convert to its three dimensional size.

### Results and Discussion

#### Effect of rare-earth element on sintering

The rare-earth-doped ceria powders were made of fine particles of about 10 nm [8]. The diameters of equivalent spherical particles, calculated from the surface areas, were 24–63 nm. The sizes of secondary particles of rare-earth-doped ceria powders were measured by a particle size distribution analyzer with

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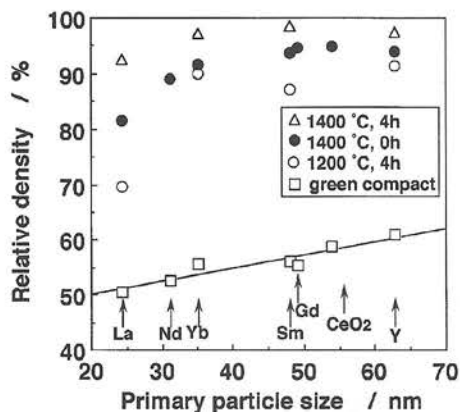


Fig. 1. Relation between diameter of equivalent primary particles and relative density of green and sintered compacts for  $\text{Ce}_{0.8}\text{R}_{0.2}\text{O}_{1.9}$  and  $\text{CeO}_2$ .

laser diffraction. The median sizes were in the range from 1.7 to 2.7  $\mu\text{m}$ . Figure 1 shows the relation between green density of powder compacts and diameter of primary particles of rare-earth-doped ceria. The green density increased linearly with increasing size of primary particles. No dependency of green density on the size of secondary particles was recognized. This result can be explained by the disappearance of open spaces formed among primary particles when the primary particle cluster with a certain size is

replaced by a dense primary particle with a same size [9, 10].

Figure 2 shows the shrinkage of rare-earth-doped and undoped ceria compacts in the temperature range from 25°C to 1400°C at the heating rate 5°C/min. The green compacts began to shrink at 600~700°C. The differential coefficient of the shrinkage with heating temperature showed a maximum at around 800°C. The shrinkage of compacts at 1400°C became larger at the higher green density. This result indicates the importance of pore size distribution on the green density and densification of powder compacts [10, 11]. When the pore size distribution approaches a monosize system, the green density increases to 74% of theoretical density. That is, a narrow pore size distribution is easy to be eliminated by sintering. Figure 1 also shows the relation between the size of primary particles and relative density of  $\text{Ce}_{0.8}\text{R}_{0.2}\text{O}_{1.9}$  and  $\text{CeO}_2$  sintered at 1200~1400°C. The relative density became higher for the higher green density, suggesting that the structure of green compact affects significantly the densification rate.

Figure 3 shows the microstructures of rare-earth-doped and undoped ceria sintered at 1600°C for 4 h. The density of all the samples was higher than 98% of theoretical density. The microstructures consisted of pentagonal or hexagonal grains of 2~7  $\mu\text{m}$ . The grain sizes of sintered samples showed a tendency to become larger with increasing ionic radius of doped-rare-earth element. No inclusion in bulk or no second phase at grain boundaries or triple points was observed by transmission electron microscopy [12]. The grains of undoped ceria grew to 50.5  $\mu\text{m}$  after the sintering at 1600°C. Doping of rare-earth element suppressed the grain growth of ceria. Inaba *et al.* explained this result by the solute drag model due to a space charge effect [6].

Figure 4 shows the effect of ionic radius [13] of rare-earth element on the diameter of primary particles, grain sizes after the sintering at 1600°C and the ratio of grain size/diameter of primary particles. The diameter of primary particles had a maximum at yttria (0.1019 nm) and decreased with increasing ionic radius of doped-rare-earth. However, the median sizes of sintered samples increased monotonously with increasing ionic radius of doped-rare-earth element. This tendency was in accordance with the change of the lattice parameters of doped ceria [8]. The grain growth rate of doped ceria was controlled by the bulk diffusion of cations, which was accelerated by doping large rare-earth element. The degree of grain growth is expressed by the ratio of grain size to diameter of primary particles. As seen in Fig. 4(c), the ratio was almost constant in the range from 0.0985 (Yb) to 0.1079 nm (Sm) of the radius of rare-earth element. Doping of Nd or La increased the degree of grain growth.

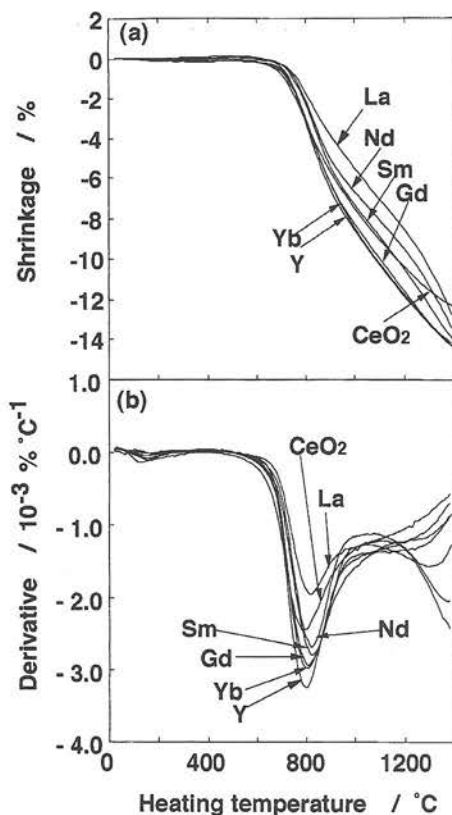


Fig. 2. Shrinkage (a) and derivative of shrinkage (b) of rare-earth-doped ceria compacts in the temperature range from 25° to 1400 °C.



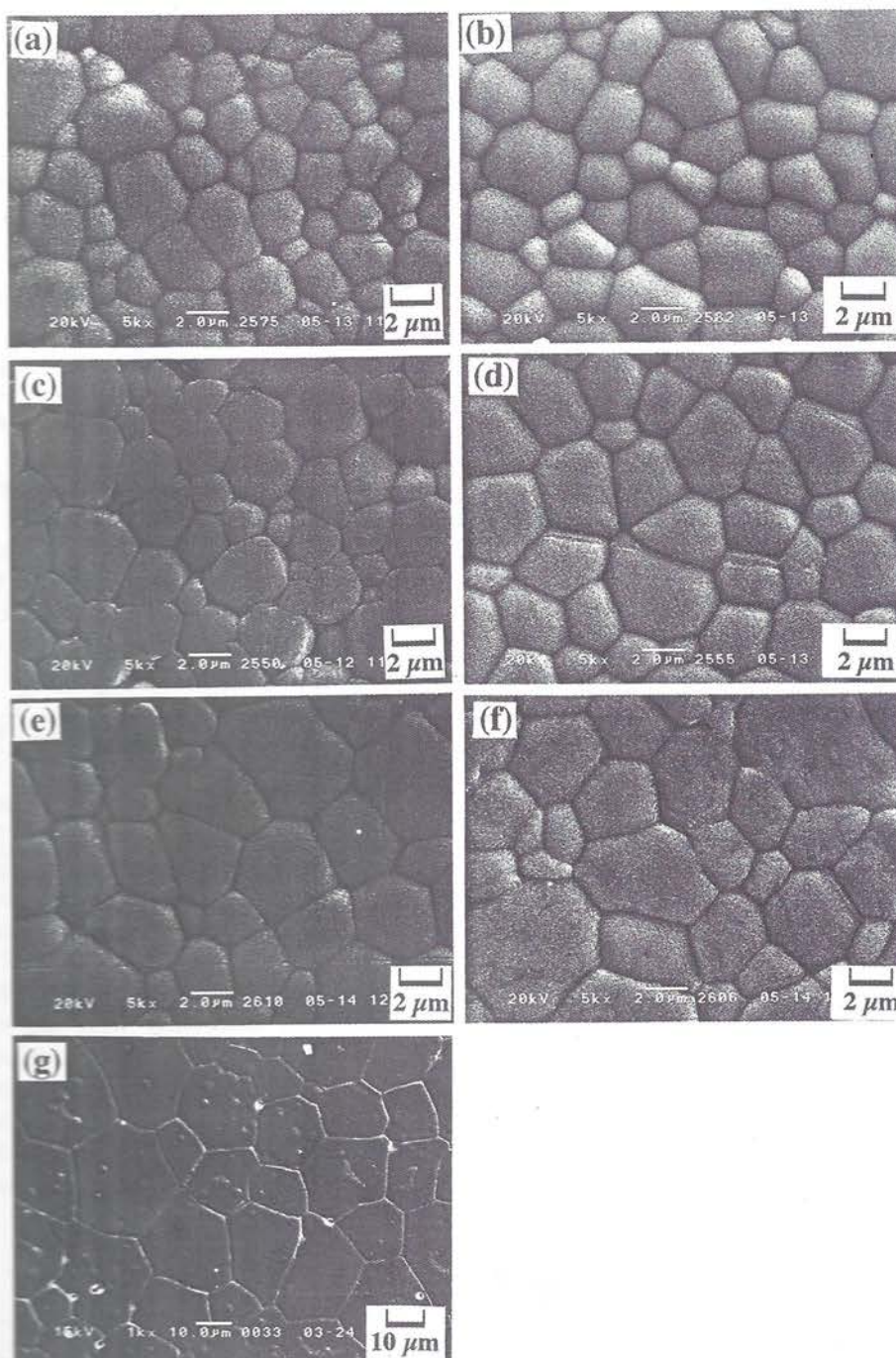


Fig. 3. Microstructures of rare-earth-doped and undoped ceria sintered at 1600°C for 4 h. (a)  $\text{Ce}_{0.8}\text{Yb}_{0.2}\text{O}_{1.9}$ , (b)  $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$ , (c)  $\text{Ce}_{0.8}\text{Gd}_{0.2}\text{O}_{1.9}$ , (d)  $\text{Ce}_{0.8}\text{Sm}_{0.2}\text{O}_{1.9}$ , (e)  $\text{Ce}_{0.8}\text{Nd}_{0.2}\text{O}_{1.9}$ , (f)  $\text{Ce}_{0.8}\text{La}_{0.2}\text{O}_{1.9}$ , (g)  $\text{CeO}_2$ .

#### Sintering mechanisms of $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$

**Theory** The shrinkage ( $\Delta L/L_0$ ) or porosity (P) in isothermal heating was analyzed based on the following five sintering mechanisms.

(I) initial stage, no grain growth, mass transport by grain boundary diffusion [14],

$$\frac{\Delta L}{L_0} = \left( \frac{NWD_b \gamma a^3}{kT} \right)^{1/3} r^{-4/3} t^{1/3} \quad (1)$$

where  $N$  is the numerical constant,  $W$  the width of

grain boundary,  $D_b$  the grain boundary diffusion coefficient,  $\gamma$  the surface energy,  $a$  the lattice spacing,  $k$  the Boltzmann's constant,  $T$  the heating temperature,  $r$  the radius of particle and  $t$  the heating time.

(II) initial stage, no grain growth, mass transport by lattice diffusion [15],

$$\frac{\Delta L}{L_0} = \left( \frac{ND_b \gamma a^3}{kT} \right)^{2/5} r^{-6/5} t^{2/5} \quad (2)$$

where  $D_b$  is the lattice diffusion coefficient.

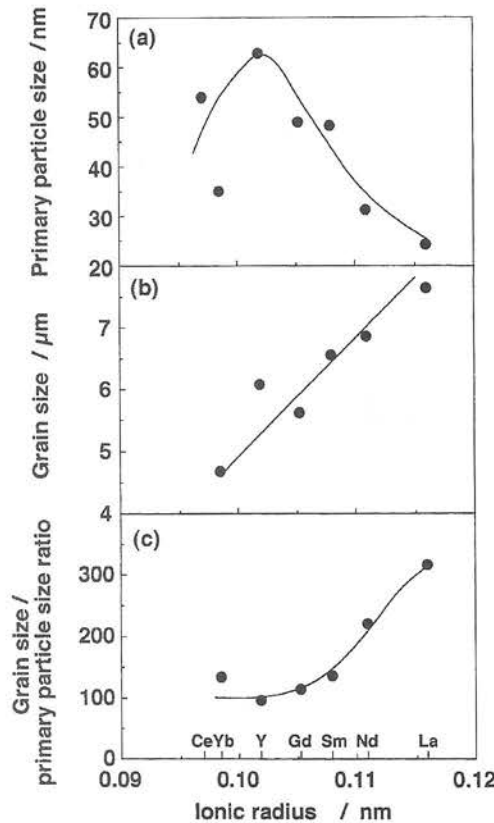


Fig. 4. Effect of ionic radius of rare-earth element on (a) the diameter of primary particles, (b) grain size after the sintering at 1600°C and (c) the ratio of grain size/diameter of primary particles.

(III) intermediate and final stage, lattice diffusion with no grain growth [16, 17],

$$\frac{dP}{dt} = \frac{C_1}{G^3 T} \quad (3)$$

which is integrated to

$$P - P_0 = \frac{C_1}{G^3 T} t \quad (4)$$

where  $P_0$  is the porosity at  $t=0$ ,  $C_1$  the constant ( $=ND_b\gamma a^3/k$ ) and  $G$  the grain size.

(IV) intermediate and final stage, lattice diffusion with grain growth [16, 17]

$$\frac{dP}{dt} = \frac{C_1}{G^3 T} \quad (5)$$

The grain size changes with the heating time, expressed by Eq. (6) [18, 19]

$$G^n - G_0^n = At \quad (6)$$

where  $G_0$  is the grain size at  $t=0$  and  $A$  is the constant. The substitution of Eq. (6) into Eq. (5) gives Eq. (7) or

Eq. (8).

$$P - P_0 = \frac{C_1}{AT} \ln \left( \frac{G_0^3 + At}{G_0^3} \right) \quad \text{for } n=3 \quad (7)$$

$$P - P_0 = \frac{C_1}{AT} \frac{n}{n-3} \left[ (G_0^n + At)^{\frac{n-3}{n}} - (G_0^n)^{\frac{n-3}{n}} \right] \quad \text{for } n \neq 3 \quad (8)$$

(V) intermediate, grain boundary diffusion with no grain growth [16, 17]

$$P = \left( \frac{C_2 t}{G^4 T} \right)^n \quad (9)$$

where  $C_2$  is the constant ( $=NWD_{gb}\gamma a^3/k$ ).

**Initial stage** In the initial stage of sintering, the following features are generally recognized: no grain growth, neck growth, and shrinkage below 5%. In the sintering at 700°C~800°C, no significant grain growth occurred. The diameter of equivalent spherical particles calculated from the specific surface area was 76 and 79 nm for 0 and 4 h, respectively, at 700°C. Similarly, the equivalent diameter was 152 and 156 nm for 0 and 4 h, respectively, at 800°C. Figure 5 shows the logarithmic relation between shrinkage and heating time at 700°C~800°C for yttria-doped ceria. The shrinkage increased nonlinearly with heating time in the logarithmic plots, indicating that the dominant sintering mechanisms changed with heating time. The slope of the curve at the initial time at 700°C was higher than 0.40 in Eq. (2), suggesting a possibility of the fast densification associated with the rearrangement of primary particles. Then, lattice diffusion contributes to the densification. The mass transport by grain boundary diffusion was not active by 2 h of heating at 700°C. The densification by grain boundary diffusion followed the mass transport by lattice diffusion at 800°C, which

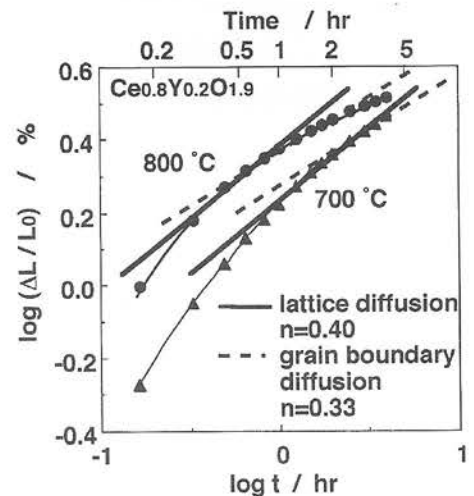


Fig. 5. Logarithmic relation between shrinkage and heating time at 700°C and 800°C for Y-doped ceria.



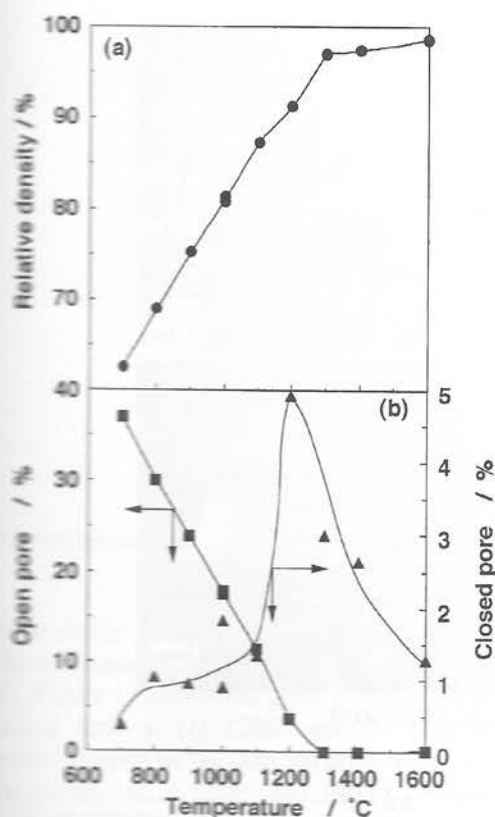


Fig. 6. Relative density (a) and porosity (b) of  $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$  heated 4 h, as a function of sintering temperature.

forms the neck between primary particles. That is, the dominant process changes from lattice diffusion to grain boundary diffusion with heating time.

**Intermediate and final stage** Figure 6(a) shows

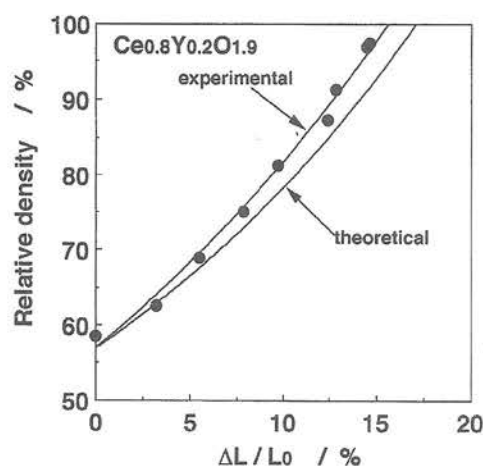


Fig. 7. Relation between shrinkage and relative density for  $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$ .

the dependence of (a) relative density and (b) porosity of  $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$  heated for 4 h on sintering temperature. The relative density increased linearly to 97% with heating to 1300°C. As shown in Fig. 6(b), the open pores disappeared at 1300°C. Therefore, the final stage of sintering started at around 1300°C. Figure 7 shows the relation between shrinkage and relative density for Y-doped ceria. When the powder compact shrinks isotatically during the sintering, the relative density ( $Y$ )–shrinkage ( $X$ ) relation is represented by Eq. (10).

$$Y = \frac{Y_0}{(1-X)^3} \quad (10)$$

where  $Y_0$  is the green density and  $X$  the shrinkage ( $\Delta L/L_0$ )

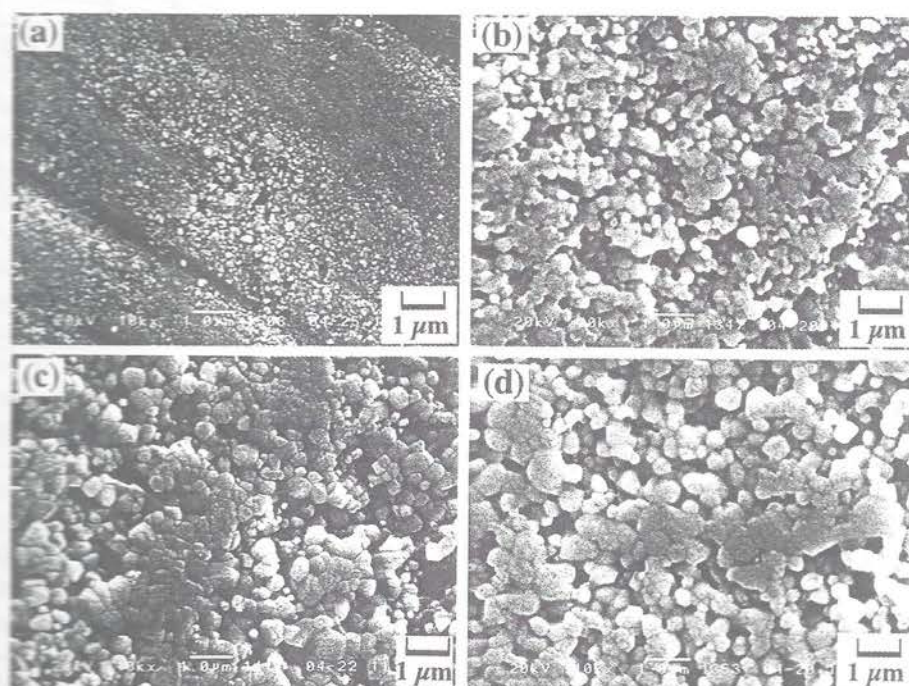


Fig. 8. Microstructures of  $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$  heated for (a) 0 h, (b) 1 h, (c) 2 h and (d) 4 h at 1200 °C.

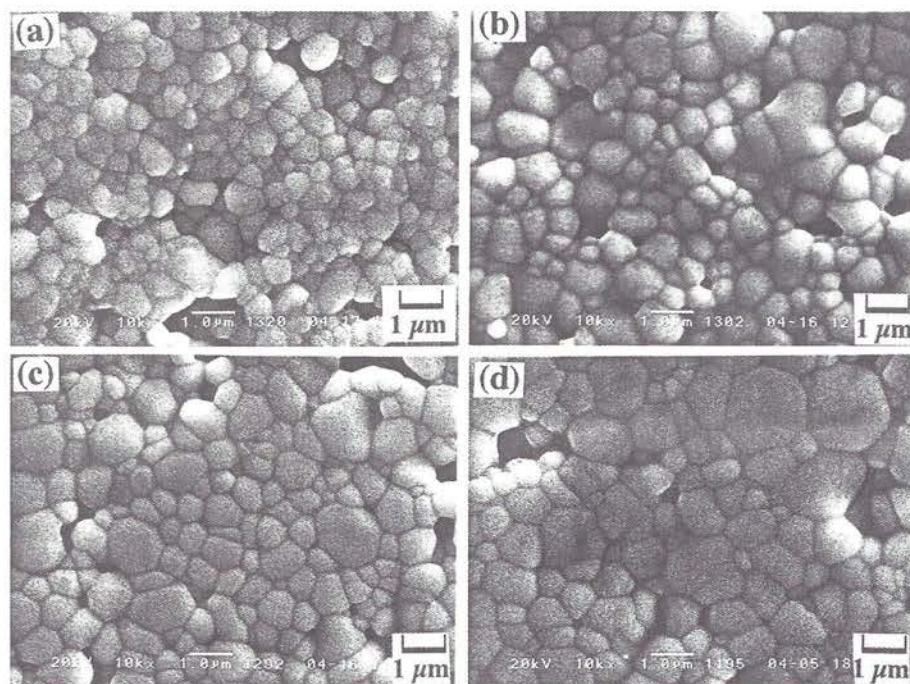


Fig. 9. Microstructures of  $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$  heated for (a) 0 h, (b) 1 h, (c) 2 h and (d) 4 h at 1400°C.

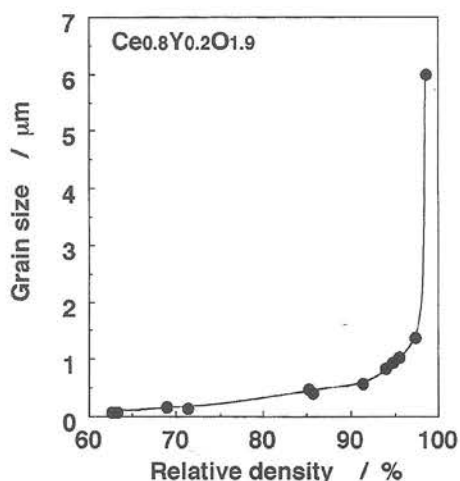


Fig. 10. Relation between grain size and relative density for Y-doped ceria.

$L_0$ ). The experimental relation was close to the theoretical prediction and approximated by Eq. (11).

$$Y = Y_0 \times 10^{0.0156X} \quad (11)$$

In the analysis of sintering mechanisms at the intermediate and final stage, the shrinkage was converted to the porosity by Eq. (11).

Figures 8 and 9 show SEM photographs of  $\text{Ce}_{0.8}\text{Y}_{0.2}\text{O}_{1.9}$  sintered at 1200° and 1400°C, respectively. The specimens were polished with 1 µm diamond paste and thermally etched before observation. The initial grain (0.06 µm) at  $t = 0$  grew to 0.57 µm after 4 h of sintering at 1200°C. Similarly, the grain size (0.83 µm) at  $t = 0$

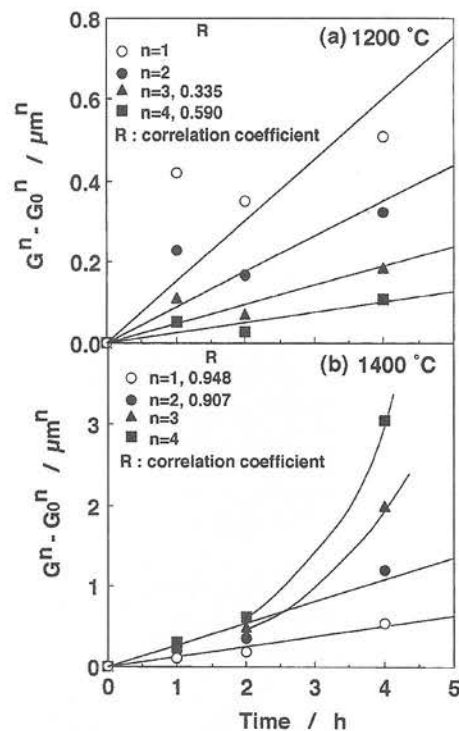


Fig. 11. Grain growth as a function of heating time at (a) 1200° and (b) 1400°C.

increased to 1.37 µm after 4 h of sintering at 1400°C. The densification at 1200° and 1400°C proceeded with grain growth. Figure 10 summarizes the relation between relative density and grain size for Y-doped ceria. The grain size became larger gradually with increasing density up to 90%. The significant grain growth was



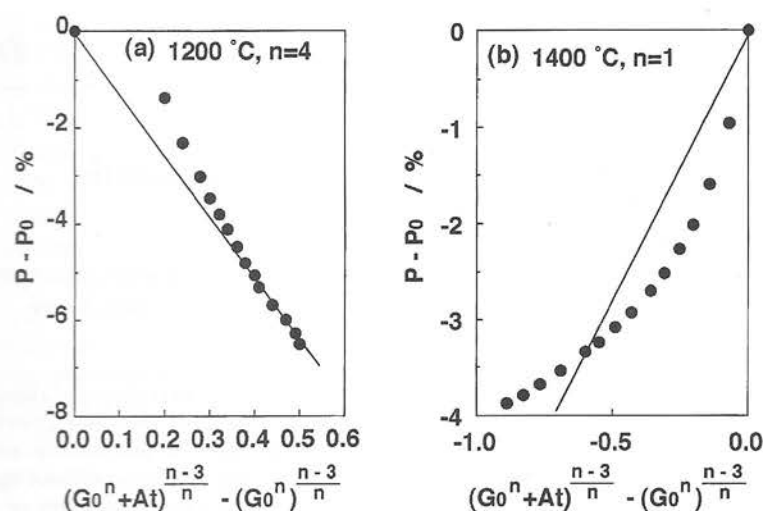


Fig. 12. Verification of the sintering mechanisms by lattice diffusion with grain growth in intermediate and final stage at 1200° and 1400°C.

measured in the final stage of sintering (density > 95 %). The mechanisms of sintering were analyzed by Eq. (6)–(8). Figure 11 shows the grain growth as a function of heating time at (a) 1200° and (b) 1400°C. The regression analysis of the data supports 4 and 1 for the  $n$  value in Eq. (6) at 1200° and 1400°C, respectively. Using these  $n$  values, the sintering mechanism by Eq. (8) was verified (Fig. 12). The linearity for the sintering at 1200°C suggests that the densification of yttria-doped ceria proceeded by the lattice diffusion with grain growth. Compared with the sintering at 1200°C, the linearity of the data was not high in the sintering at 1400°C.

### Conclusions

The green density of rare-earth-doped ceria ( $\text{Ce}_{0.8}\text{R}_{0.2}\text{O}_{2-x}$ ,  $\text{R}=\text{Yb}$ ,  $\text{Y}$ ,  $\text{Gd}$ ,  $\text{Sm}$ ,  $\text{Nd}$  and  $\text{La}$ ) increased with increasing diameter of primary particles. The densification rate was greatly dominated by the green density and higher for the higher green density. The powder compacts were densified above 98% relative density by the sintering at 1600°C for 4 h. The grain sizes (4.7–7.6  $\mu\text{m}$ ) of samples showed a tendency to become larger with increasing ionic radius of doped-rare-earth element. The grains of undoped ceria grew to 50.5  $\mu\text{m}$  after the sintering at 1600°C. Doping of rare-earth element suppressed the grain growth of ceria. The dominant mechanisms of densification in the initial stage of sintering at 700°–800°C changed with heating time as follows: particle rearrangement  $\rightarrow$  lattice diffusion  $\rightarrow$  grain boundary diffusion. The densification at 1200° and 1400°C proceeded with grain growth. The density during the sintering decreased by mass transport

through the lattice diffusion with grain growth.

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